#### **Machine Learning Systems**

Lecture 9: Convolutional Neural Networks (CNNs, ConvNets)

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CSCE 585: Machine Learning Systems | Fall 2022 | https://pooyanjamshidi.github.io/mls/

## Convolutional Neural Networks (CNNs, ConvNets)

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#### Partially based on:

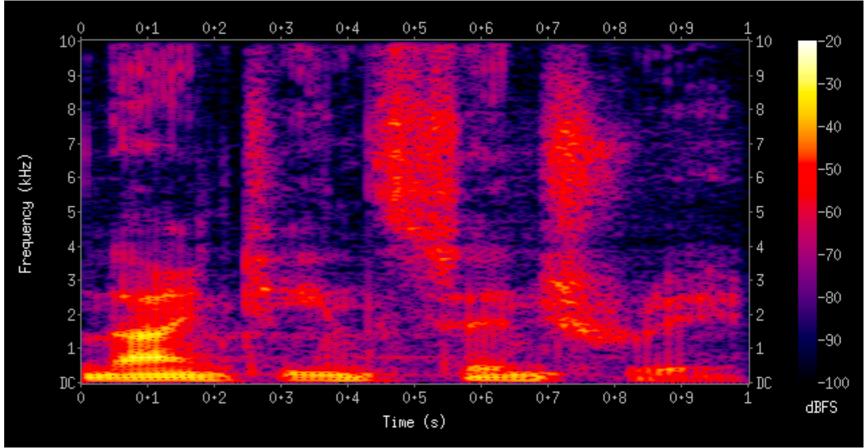
- Chapter 9 of the *Deep Learning Book:* <a href="https://www.deeplearningbook.org/">https://www.deeplearningbook.org/</a>
- CS231n Convolutional Neural Networks for Visual Recognition

#### Convolutional Networks

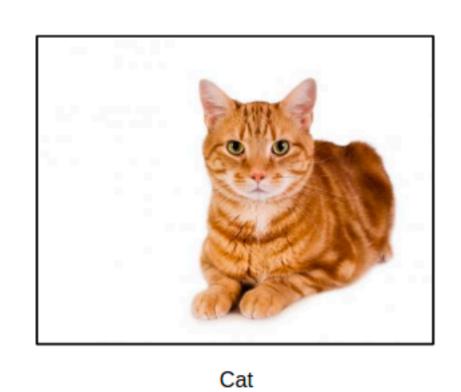
- Scale up neural networks to process very large images / video sequences
  - Sparse connections
  - Parameter sharing
- Automatically generalize across spatial translations of inputs
- Applicable to any input that is laid out on a grid (1-D, 2-D, 3-D, ...)

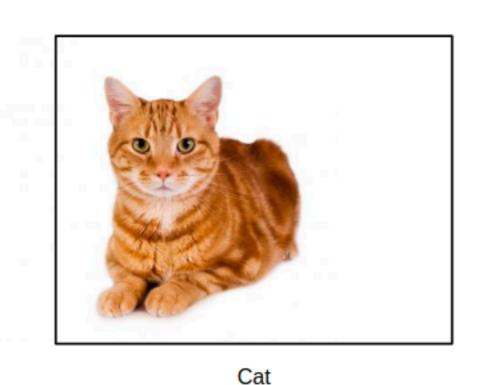
#### Examples of Grid Structures





## Shift Invariance in Convolutional Neural Networks





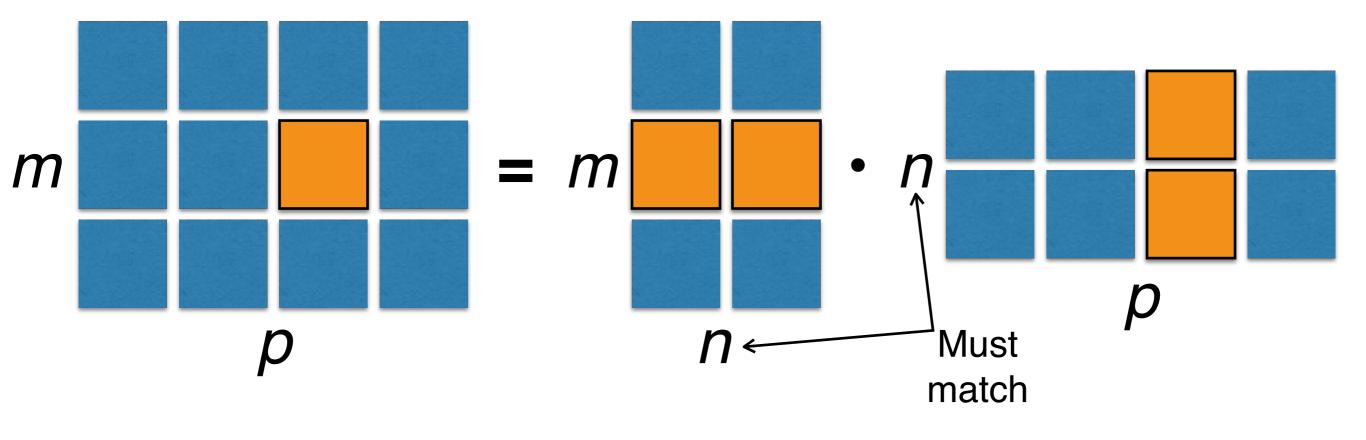
## Key Idea

- Replace matrix multiplication in neural nets with convolution
- Everything else stays the same
  - Maximum likelihood
  - Back-propagation
  - · etc.

### Matrix (Dot) Product

$$C = AB. (2.4)$$

$$C_{i,j} = \sum_{k} A_{i,k} B_{k,j}. \tag{2.5}$$



$$(\mathbf{A}^{\top})_{i,j} = A_{j,i}. \tag{2.3}$$

$$(\boldsymbol{A}\boldsymbol{B})^{\top} = \boldsymbol{B}^{\top}\boldsymbol{A}^{\top}. \tag{2.9}$$

#### 2D Convolution

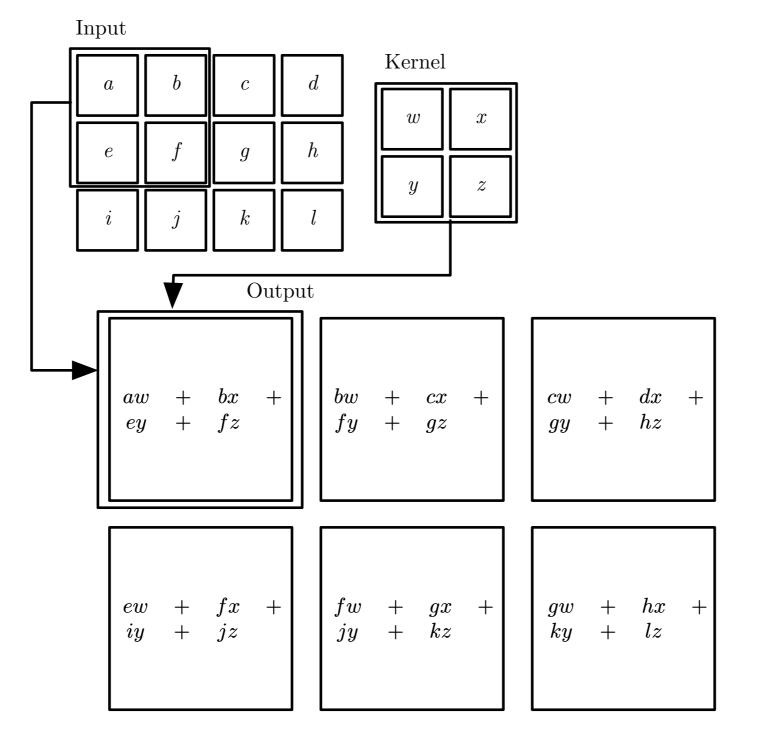


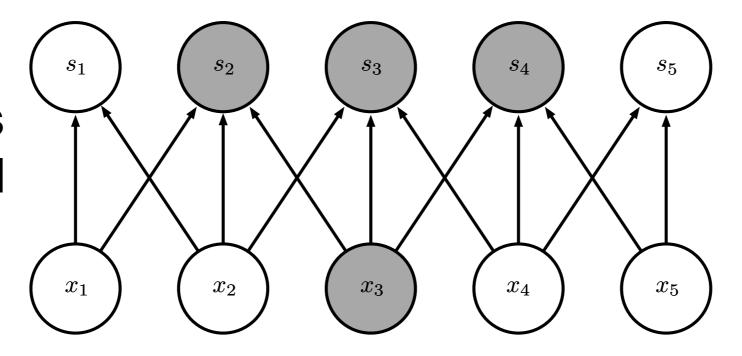
Figure 9.1

### Three Operations

- Convolution: like matrix multiplication
  - Take an input, produce an output (hidden layer)
- "Deconvolution": like multiplication by transpose of a matrix
  - Used to back-propagate error from output to input
  - Reconstruction in autoencoder / RBM
- Weight gradient computation
  - Used to backpropagate error from output to weights
  - Accounts for the parameter sharing

## Sparse Connectivity

Sparse connections due to small convolution kernel



Dense connections

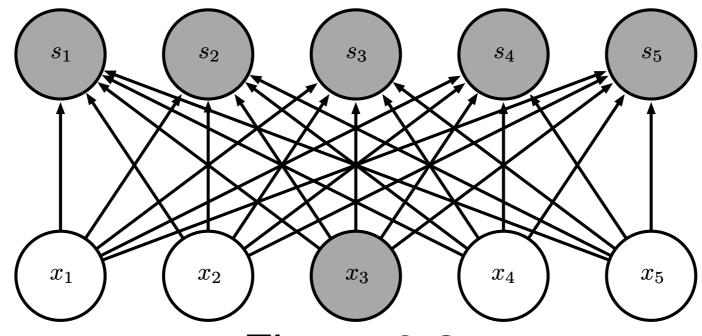
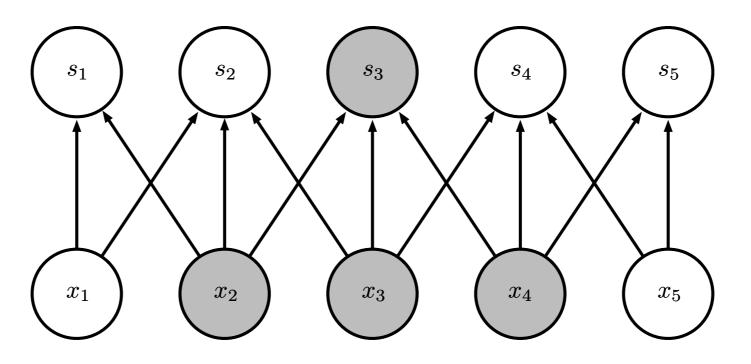


Figure 9.2

## Sparse Connectivity

Sparse connections due to small convolution kernel



Dense connections

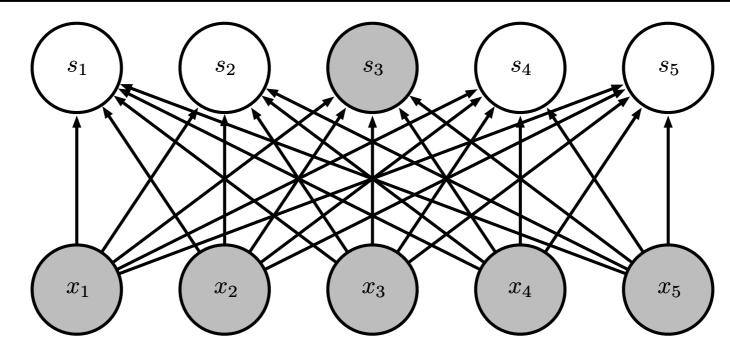


Figure 9.3

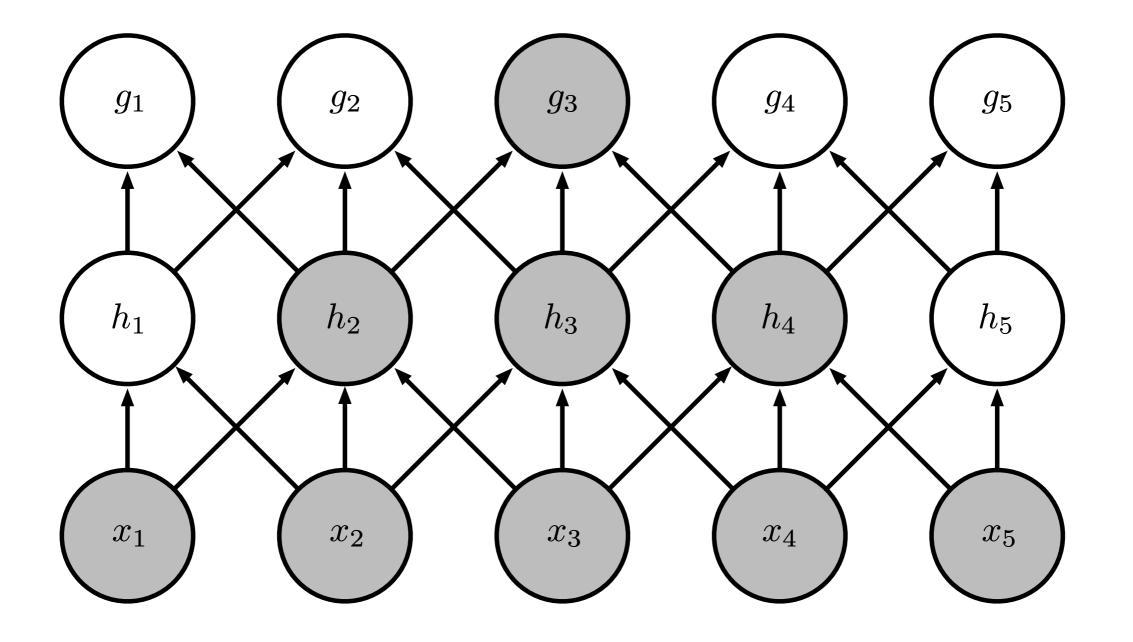
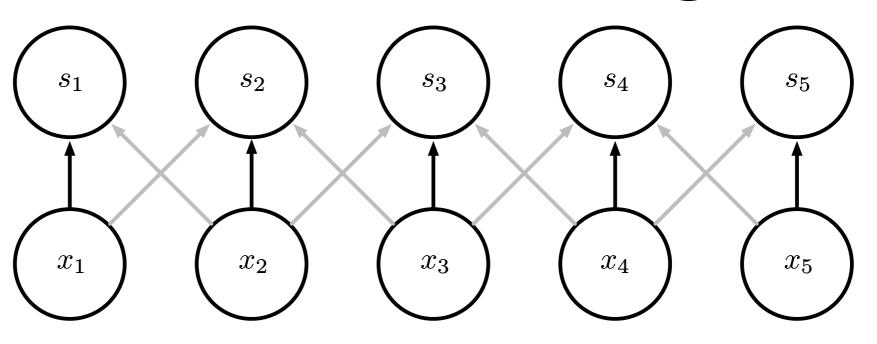


Figure 9.4

## Parameter Sharing

Convolution shares the same parameters across all spatial locations



Traditional matrix multiplication does not share any parameters

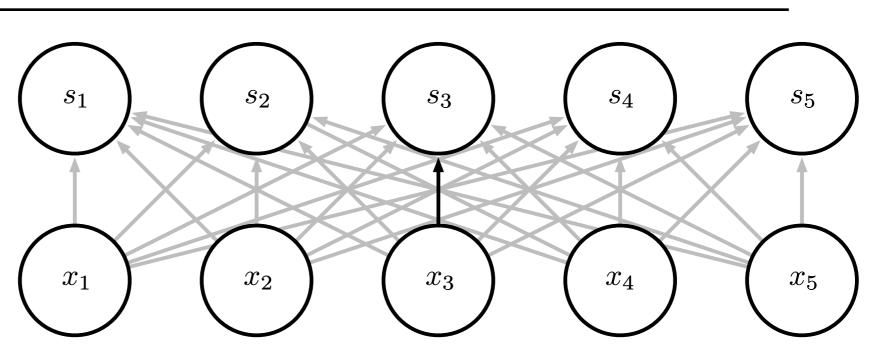


Figure 9.5

## Edge Detection by Convolution

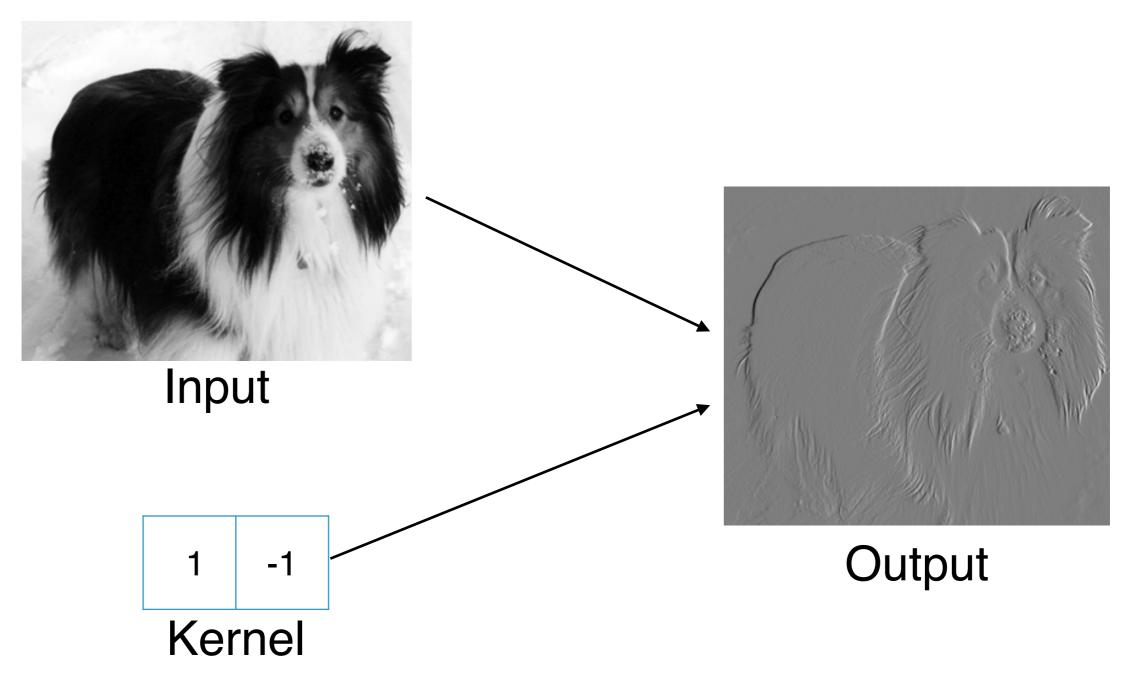


Figure 9.6

### Efficiency of Convolution

Input size: 320 by 280

Kernel size: 2 by 1

Output size: 319 by 280

Stored floats
Float muls or adds

### Efficiency of Convolution

Input size: 320 by 280

Kernel size: 2 by 1

Output size: 319 by 280

	Convolution	Dense matrix	Sparse matrix
Stored floats	2	319*280*320*28 0 > 8e9	2*319*280 = 178,640
Float muls or adds	319*280*3 = 267,960	> 16e9	Same as convolution (267,960)

# Convolutional Network Components

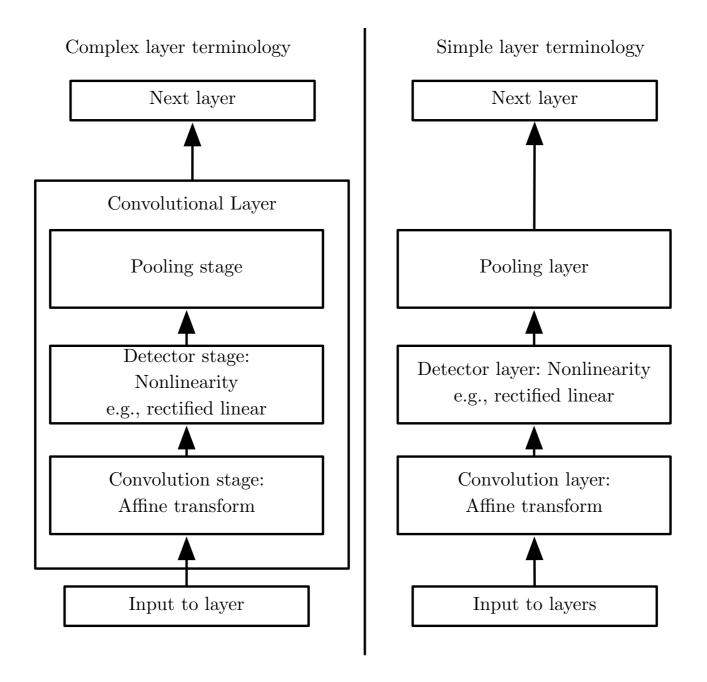
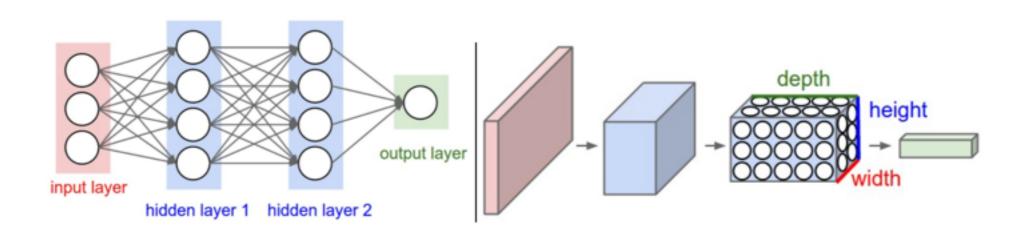


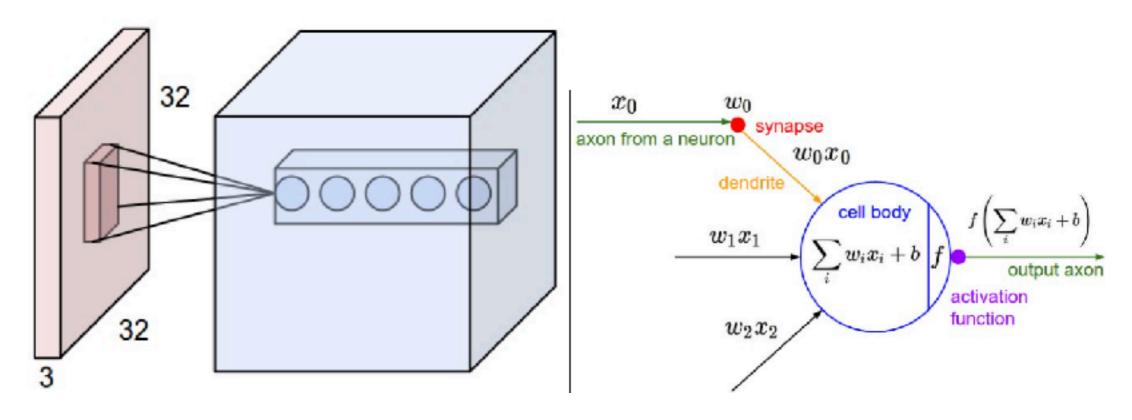
Figure 9.7

## Regular fully-connected NN vs ConvNet



A ConvNet is made up of Layers. Every Layer has a simple API: It transforms an input 3D volume to an output 3D volume with some differentiable function that may or may not have parameters.

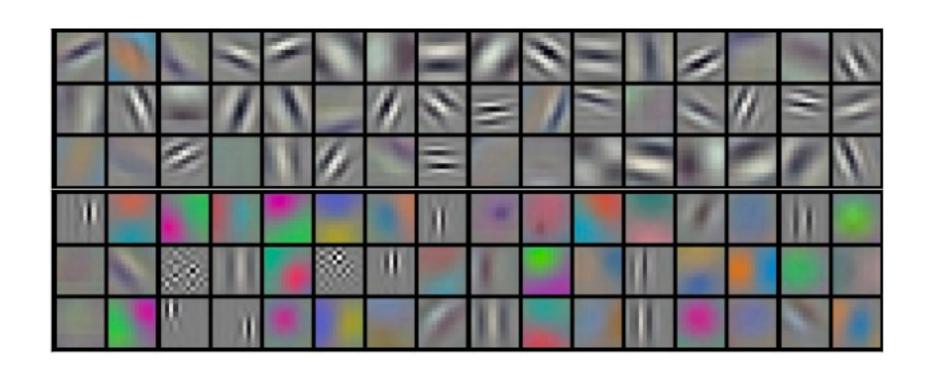
## Local Connectivity



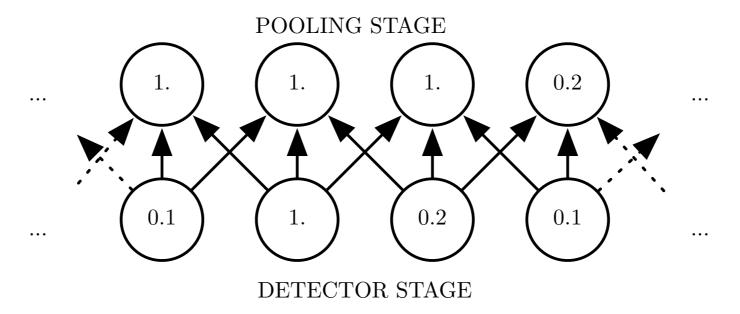
Example 1. For example, suppose that the input volume has size [32x32x3], (e.g. an RGB CIFAR-10 image). If the receptive field (or the filter size) is 5x5, then each neuron in the Conv Layer will have weights to a [5x5x3] region in the input volume, for a total of 5\*5\*3 = 75 weights (and +1 bias parameter). Notice that the extent of the connectivity along the depth axis must be 3, since this is the depth of the input volume.

Example 2. Suppose an input volume had size [16x16x20]. Then using an example receptive field size of 3x3, every neuron in the Conv Layer would now have a total of 3\*3\*20 = 180 connections to the input volume. Notice that, again, the connectivity is local in space (e.g. 3x3), but full along the input depth (20).

### Example of learned kernels



#### Max Pooling and Invariance to Translation



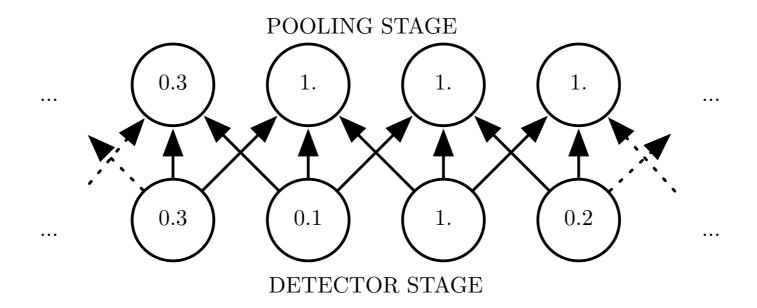


Figure 9.8

## Cross-Channel Pooling and Invariance to Learned Transformations

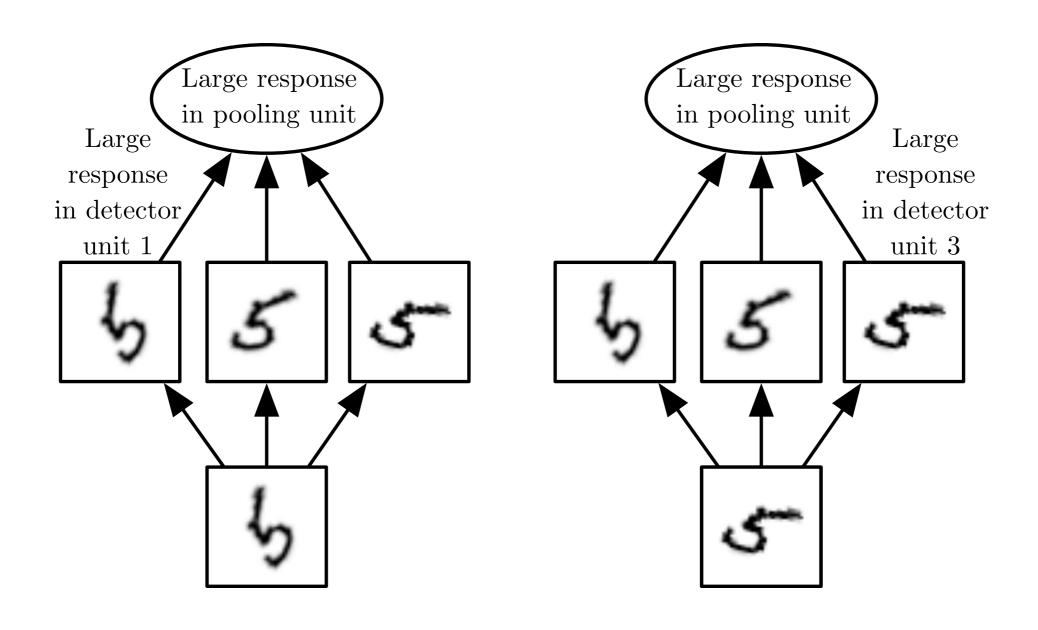


Figure 9.9

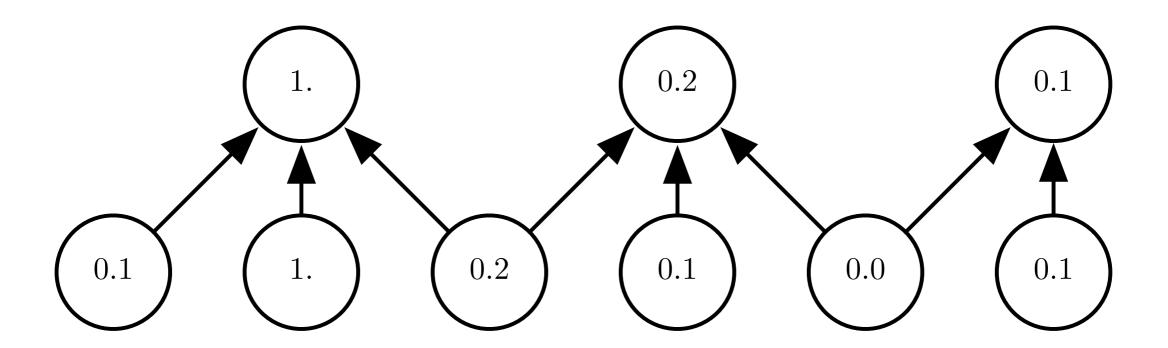
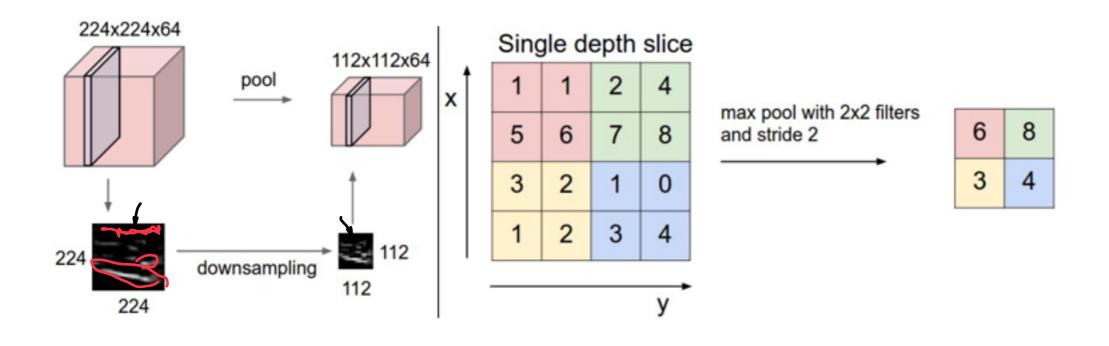


Figure 9.10

# Pooling layer downsamples the volume spatially



## Example Classification Architectures

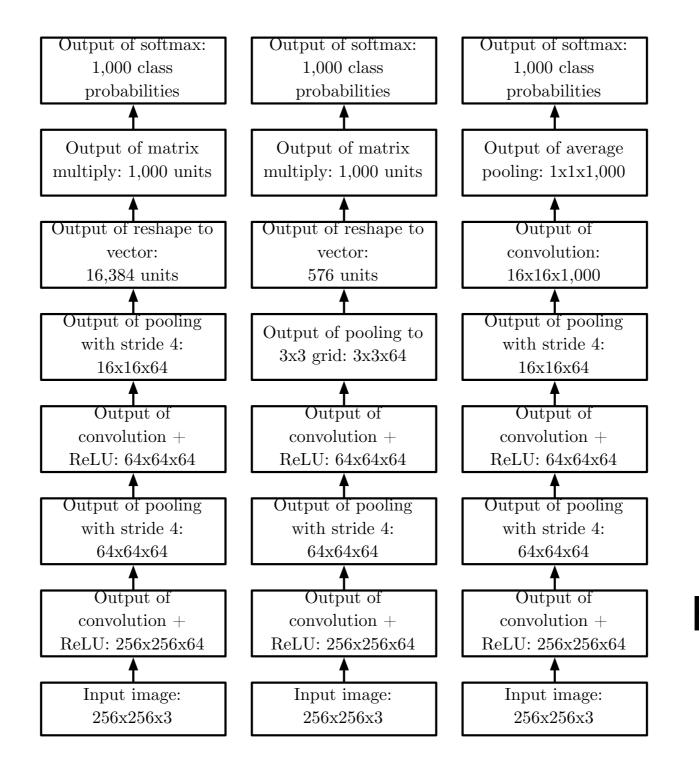
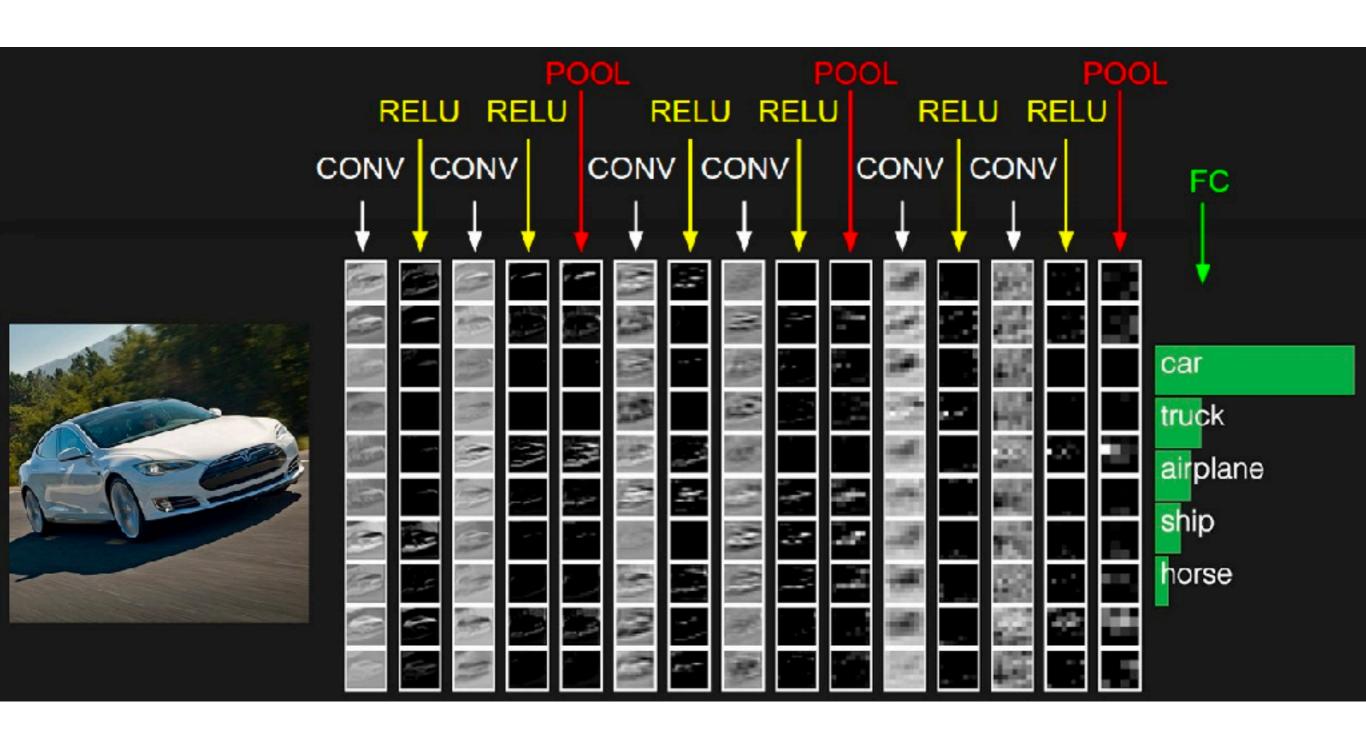


Figure 9.11

#### ConvNet architecture



## Architecture Overview of ConvNets

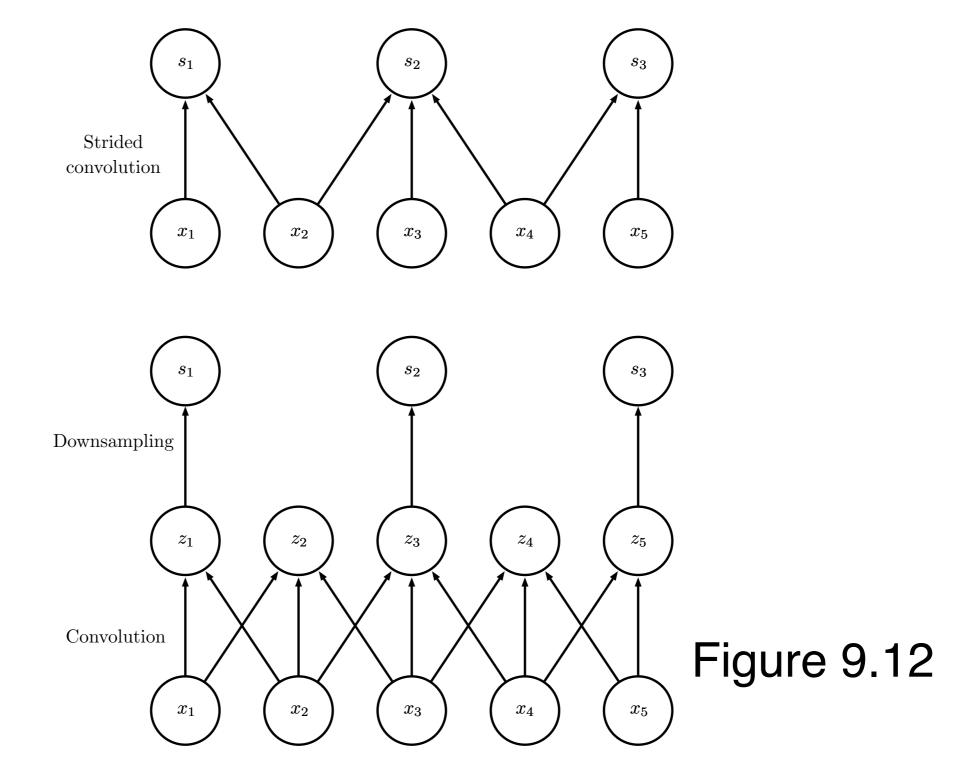
[INPUT - CONV - RELU - POOL - FC]

- INPUT [32x32x3] will hold the raw pixel values of the image, in this case an image of width 32, height 32, and with three color channels R,G,B.
- CONV layer will compute the output of neurons that are connected to local regions in the input, each
  computing a dot product between their weights and a small region they are connected to in the input volume.
   This may result in volume such as [32x32x12] if we decided to use 12 filters.
- RELU layer will apply an elementwise activation function, such as the max(0, x) thresholding at zero. This
  leaves the size of the volume unchanged ([32x32x12]).
- POOL layer will perform a downsampling operation along the spatial dimensions (width, height), resulting in volume such as [16x16x12].
- FC (i.e. fully-connected) layer will compute the class scores, resulting in volume of size [1x1x10], where each
  of the 10 numbers correspond to a class score, such as among the 10 categories of CIFAR-10. As with
  ordinary Neural Networks and as the name implies, each neuron in this layer will be connected to all the
  numbers in the previous volume.

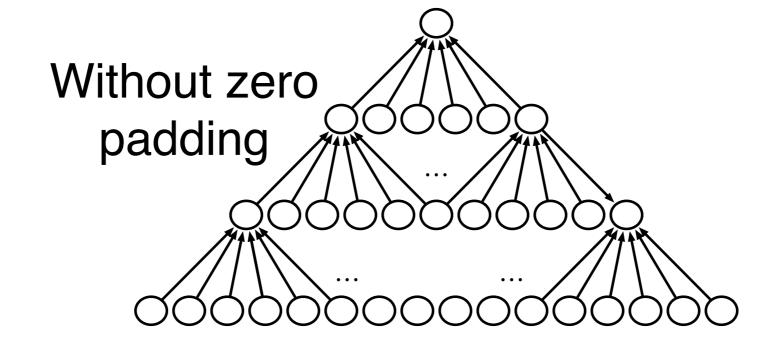
## Architecture Overview of ConvNets

- A ConvNet architecture is in the simplest case a list of Layers that transform the image volume into an output volume (e.g. holding the class scores)
- There are a few distinct types of Layers (e.g. CONV/FC/RELU/POOL are by far the most popular)
- Each Layer accepts an input 3D volume and transforms it to an output 3D volume through a differentiable function
- Each Layer may or may not have parameters (e.g. CONV/FC do, RELU/POOL don't)
- Each Layer may or may not have additional hyperparameters (e.g. CONV/FC/POOL do, RELU doesn't)

#### Convolution with Stride



### Zero Padding Controls Size



With zero padding

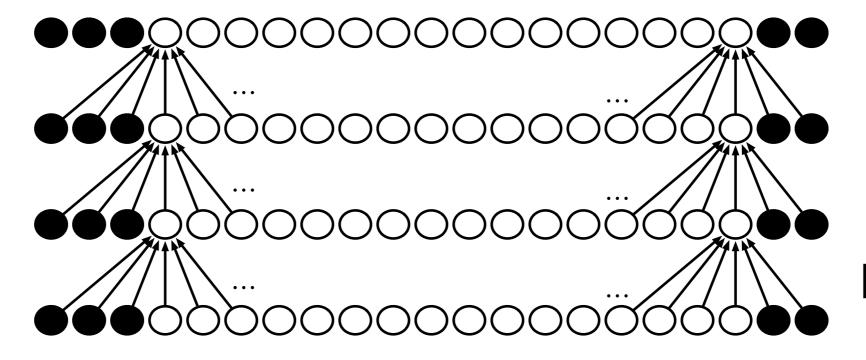
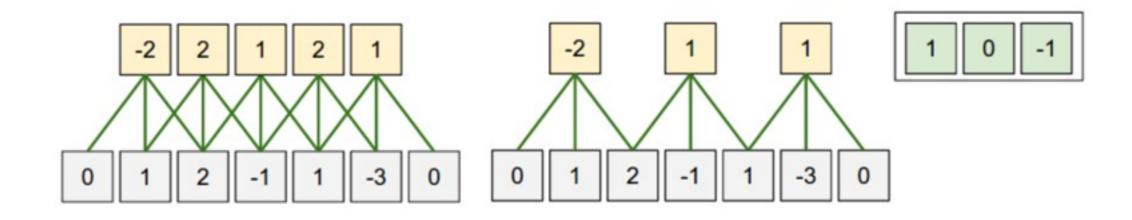


Figure 9.13

# Output size with zero padding and stride



## Kinds of Connectivity

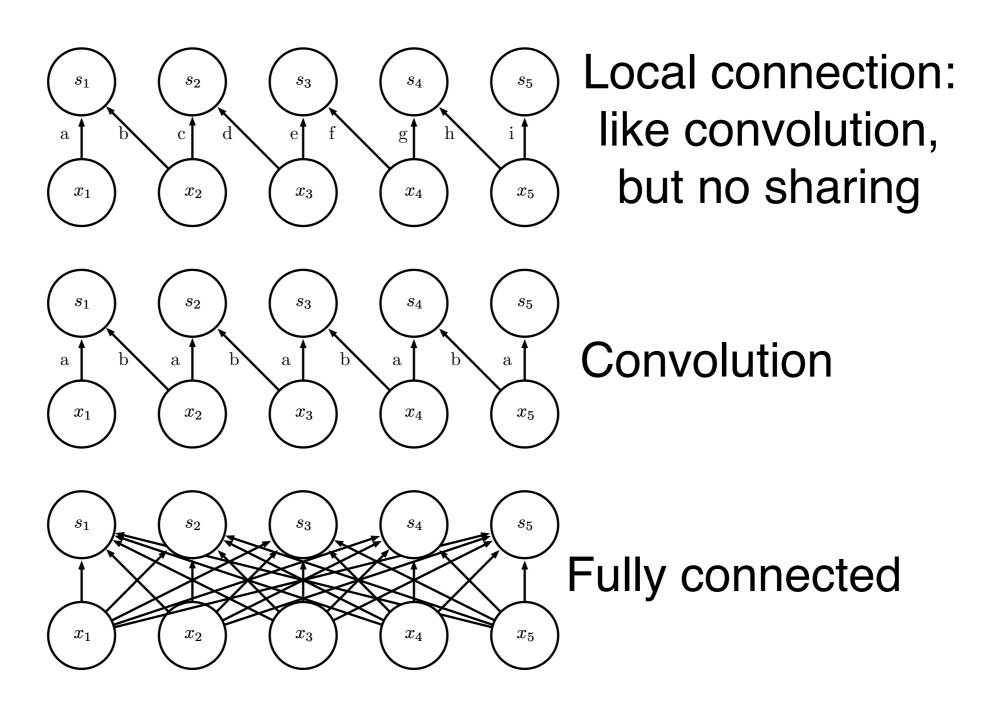


Figure 9.14

#### Partial Connectivity Between Channels

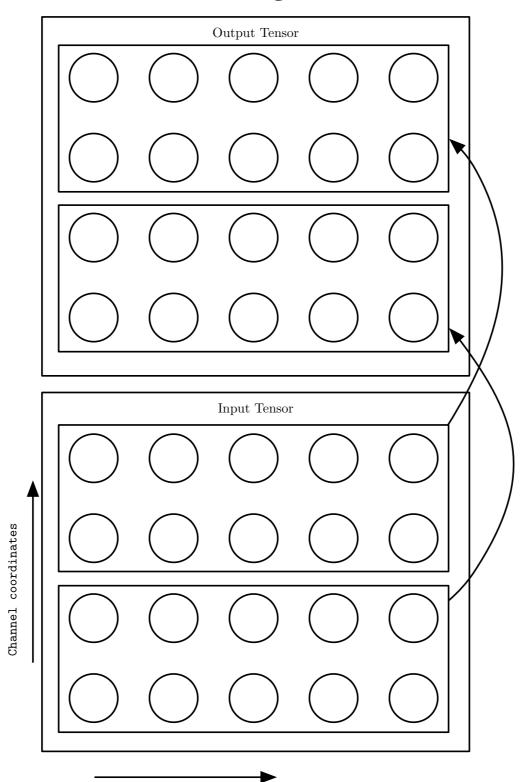


Figure 9.15

Spatial coordinates

#### Tiled convolution

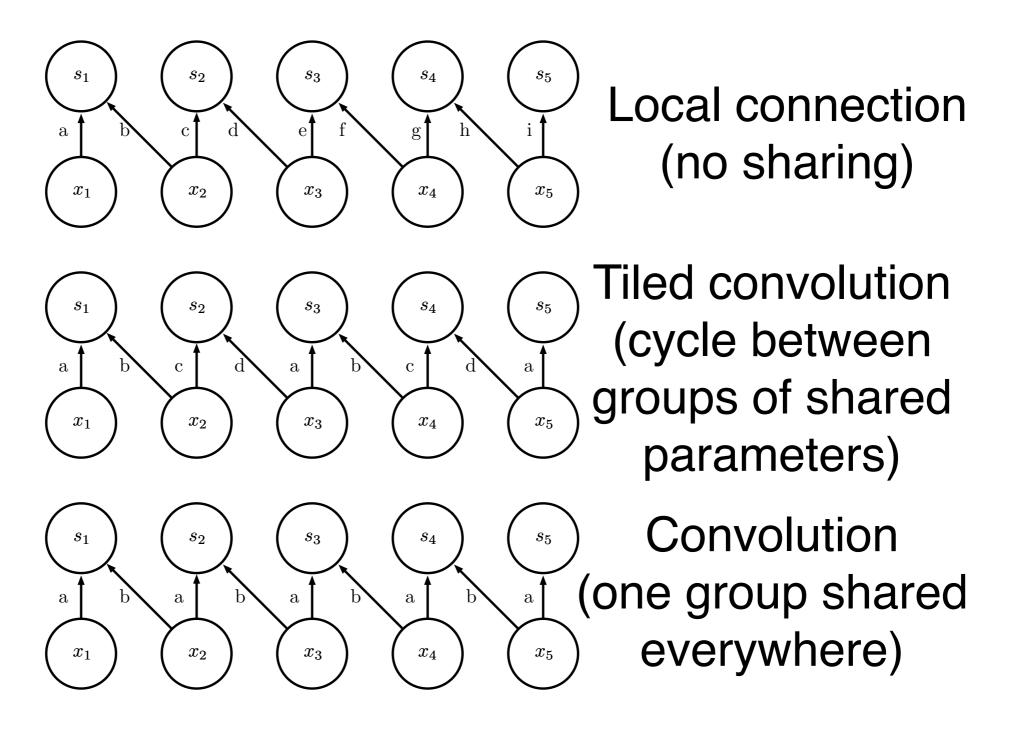
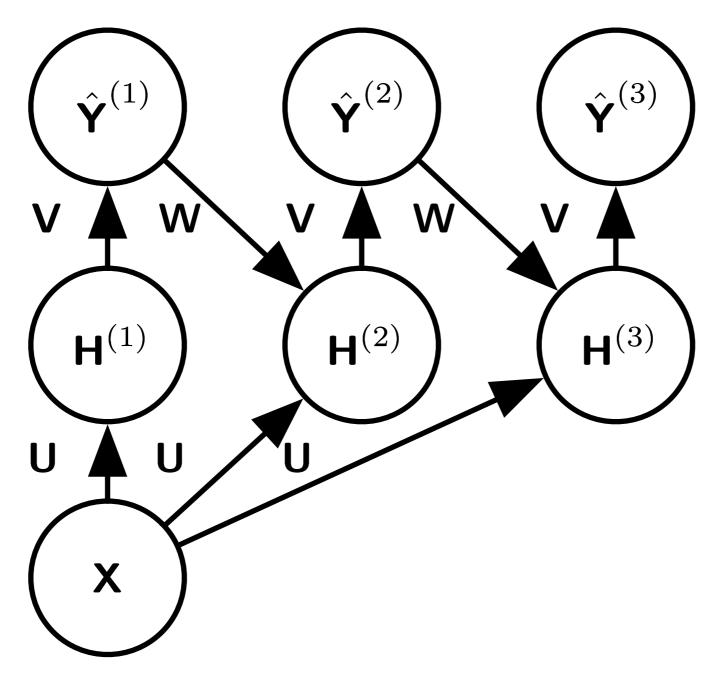
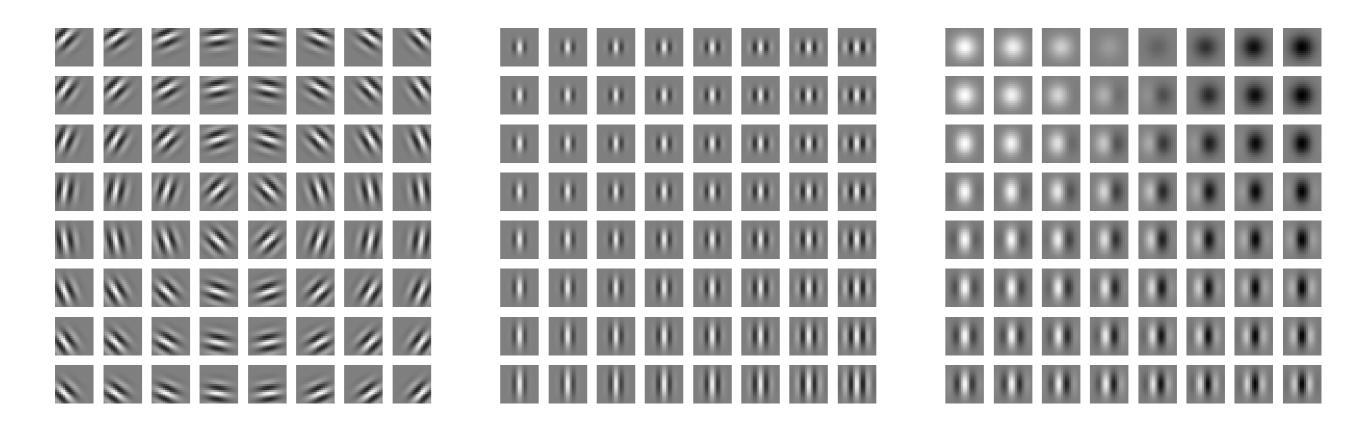


Figure 9.16

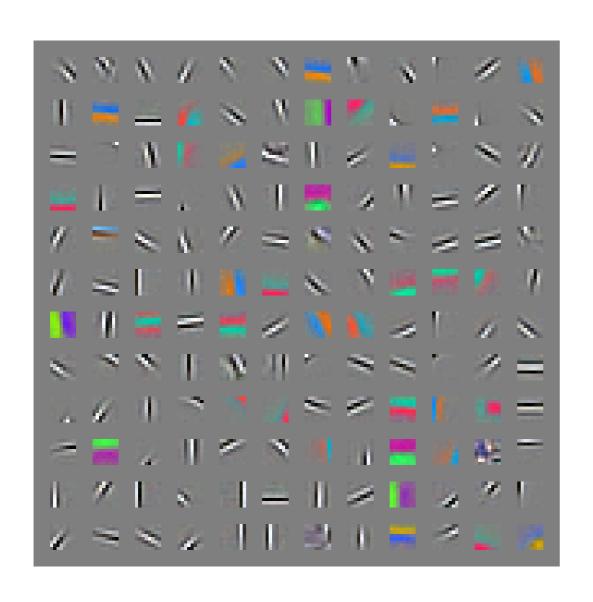
### Recurrent Pixel Labeling

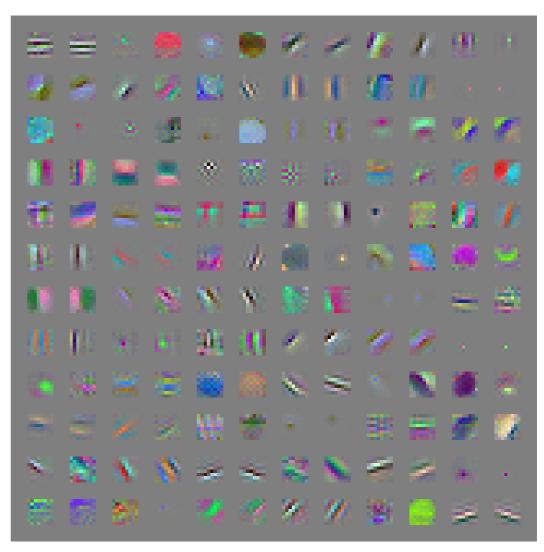


#### Gabor Functions



#### Gabor-like Learned Kernels





### Major Architectures

- Spatial Transducer Net: input size scales with output size, all layers are convolutional
- All Convolutional Net: no pooling layers, just use strided convolution to shrink representation size
- Inception: complicated architecture designed to achieve high accuracy with low computational cost
- ResNet: blocks of layers with same spatial size, with each layer's output added to the same buffer that is repeatedly updated. Very many updates = very deep net, but without vanishing gradient.